

### Compound interest:

Total amt after n years:

$$A = P \left( 1 + \frac{r}{100} \right)^n$$

Simple interest:

Total interest after t

$$\text{years: } I = \frac{PRT}{100}$$

### Mensuration:

(\*csa= curved surface area)

$$\text{csa of cone} = \pi r l$$

$$\text{csa of sphere} = 4\pi r^2$$

$$\text{csa of cylinder} = 2\pi r h$$

$$\text{vol of cone} = \frac{1}{3}\pi r^2 h$$

$$\text{vol of sphere} = \frac{4}{3}\pi r^3$$

$$\text{vol of cylinder} = \pi r^2 h$$

$$\text{Area of circle} = \pi r^2$$

$$\text{Cir of circle} = 2\pi r$$

$$\text{Arc Length}(r) = r\theta$$

$$\text{Area of sector}(r) = \frac{1}{2}r^2\theta$$

$$\text{Arc Length}(\theta) = \frac{x}{360} \times 2\pi r$$

$$\text{Area of sector}(\theta) = \frac{x}{360} \times \pi r^2$$

### Similar Figures:

$$\text{Ratio of length} = \frac{l_1}{l_2}$$

$$\text{Ratio of area} = \left(\frac{l_1}{l_2}\right)^2$$

$$\text{Ratio of volume} = \left(\frac{l_1}{l_2}\right)^3$$

### Trigonometry:

$$\sin \theta = \frac{\text{opp}}{\text{hypo}}$$

$$\cos \theta = \frac{\text{adj}}{\text{hypo}}$$

$$\tan \theta = \frac{\text{opp}}{\text{adj}}$$

### Pythagoras theorem:

$$c^2 = a^2 + b^2$$

### Sine rule:

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

### Cosine rule:

$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$\cos A = \frac{b^2 + c^2 - a^2}{2bc}$$

### Coordinate Geometry:

length=

$$\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$\text{gradient of AB} = \frac{y_2 - y_1}{x_2 - x_1}$$

$$y - y_1 = m(x - x_1)$$

$$\text{eq of line AB: } y = mx + c$$

$$\text{Area of } \Delta = \frac{1}{2} ab \sin C$$

### Statistics :

$$\text{Mean} = \frac{\sum fx}{\sum f}$$

$$\text{SD} = \sqrt{\frac{\sum fx^2}{\sum f} - \left(\frac{\sum fx}{\sum f}\right)^2}$$

Lower q= 25<sup>th</sup> percentile

Median = 50<sup>th</sup> percentile

Upper q= 75<sup>th</sup> percentile

Interquartile range=

upper q - lower q

### Quadratic equation:

$$(a+b)^2 = a^2 + 2ab + b^2$$

$$(a-b)^2 = a^2 - 2ab + b^2$$

$$a^2 - b^2 = (a + b)(a - b)$$

### Congruency Tests

1) SSS 2) SAS(included  $\sphericalangle$ )

3) AAS 4) ASA 5) RHS

### Similarity Tests

1) Ratio of sides are equal

2) AAA

3) SAS(included  $\sphericalangle$ )

### Quadratic equation:

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$ax^2 + bx + c = 0$$

**Case 1:**  $b^2 - 4ac > 0$

two distinct real roots.

**Case 2:**  $b^2 - 4ac = 0$

Two real and equal roots.

**Case 3:**  $b^2 - 4ac < 0$

no real roots.

$$\text{Sum of roots: } \alpha + \beta = -\frac{b}{a}$$

$$\text{Product of roots: } \alpha\beta = \frac{c}{a}$$

Quadratic equation:

$$x^2 - (\text{sum of roots})x +$$

$$(\text{product of roots}) = 0$$

Quadratic inequalities:

$$(x - a)(x - b) < 0 \rightarrow a < x < b, b > a$$

$$(x - a)(x - b) > 0 \rightarrow x < a \text{ or } x > b$$

For  $ax^2 + bx + c > 0$  ( $a > 0$ )

and  $ax^2 + bx + c < 0$  ( $a < 0$ ),

then  $b^2 - 4ac < 0$ .

### Cubic equations:

$$a^3 + b^3 = (a+b)(a^2 - ab + b^2)$$

$$a^3 - b^3 = (a-b)(a^2 + ab + b^2)$$

### Law of Indices

$$(a) a^m \times a^n = a^{m+n}$$

$$(b) a^m \div a^n = a^{m-n}$$

$$(c) (a^m)^n = a^{mn}$$

$$(d) a^m \times b^m = (ab)^m$$

$$a^m \div b^m = \left(\frac{a}{b}\right)^m$$

$$(e) a^0 = 1$$

$$(g) a^{-n} = \frac{1}{a^n}$$

$$(h) \left(\frac{a}{b}\right)^{-m} = \left(\frac{b}{a}\right)^m$$

$$(i) a^{\frac{1}{n}} = \sqrt[n]{a}$$

$$(j) a^{\frac{m}{n}} = \left(\sqrt[n]{a}\right)^m$$

### Operations on surds

$$a\sqrt{x} + b\sqrt{x} = (a + b)\sqrt{x}$$

$$a\sqrt{x} - b\sqrt{x} = (a - b)\sqrt{x}$$

$$(\sqrt{x})(\sqrt{y}) = \sqrt{(xy)}$$

$$\frac{\sqrt{x}}{\sqrt{y}} = \sqrt{\frac{x}{y}}$$

### Rationalizing the denominator

$$(a) \frac{\sqrt{x}}{\sqrt{y}} = \frac{\sqrt{x}}{\sqrt{y}} \times \frac{\sqrt{y}}{\sqrt{y}} = \frac{\sqrt{xy}}{y}$$

$$(b) \frac{1}{\sqrt{x} + \sqrt{y}} = \frac{1}{\sqrt{x} + \sqrt{y}} \times \frac{\sqrt{x} - \sqrt{y}}{\sqrt{x} - \sqrt{y}} = \frac{\sqrt{x} - \sqrt{y}}{x - y}$$

### Logarithms

If  $a^x = b, a > 0$

then  $\log_a b = x$

Laws of Logarithms

$$(a) \log_a xy = \log_a x + \log_a y$$

$$(b) \log_a \frac{x}{y} = \log_a x - \log_a y$$

$$(c) \log_a (x)^n = n \log_a x$$

$$(d) \log_a 1 = 0$$

$$(e) \log_a a = 1$$

$$(f) \log_a x = \frac{\log_b x}{\log_b a}$$

$$\log_a x = \frac{1}{\log_x a}$$

Note :  $\log_a x$  exists if  $a > 0$

and  $x > 0$ .

### Coordinate Geometry

Area of  $\Delta ABC$

$$= \frac{1}{2} \begin{vmatrix} x_1 & x_2 & x_3 & x_1 \\ y_1 & y_2 & y_3 & y_1 \end{vmatrix}$$

$$= \frac{1}{2} (x_1 y_2 + x_2 y_3 + x_3 y_1 - x_2 y_1 - x_3 y_2 - x_1 y_3)$$

Midpoint  $M$ ,

$$\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$$

For two lines  $l_1$  and  $l_2$ ,

(a)  $l_1$  is parallel to  $l_2$

$\rightarrow$  their gradients are equal

(b)  $l_1$  is perpendicular to  $l_2$

$\rightarrow$  the product of their

gradients is -1.

### Circles

centre (a,b), radius r

Equation of circle:

$$(x - a)^2 + (y - b)^2 = r^2$$

### The Binomial Theorem

$$(x + y)^n =$$

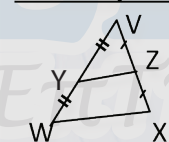
$$x^n + \binom{n}{1} x^{n-1} y +$$

$$\binom{n}{2} x^{n-2} y^2 + \binom{n}{3} x^{n-3} y^3 +$$

$$\dots + \binom{n}{r} x^{n-r} y^r + \dots + y^n$$

$$(r + 1)^{\text{th}} \text{ term} = \binom{n}{r} x^{n-r} y^r$$

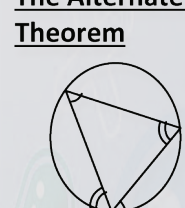
### The Midpoint Theorem



Y and Z are the midpoints of VW and VX respectively.

Result:  $YZ \parallel WX, YZ = \frac{1}{2} WX$

### The Alternate Segment Theorem



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& MATH  
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